

# Parametric study of recuperative VOC oxidation reactor with porous media

N.N. Gnesdilov\*, K.V. Dobrego, I.M. Kozlov

*Heat and Mass Transfer Institute, National Academy of Sciences of Belarus, P. Brovki Street 15, Minsk 220072, Belarus*

Received 9 October 2006

Available online 16 January 2007

## Abstract

Numerical study of volatile organic compounds (VOC) oxidation reactor consisting of two coaxial tubes, filled with inert porous media is performed. Influence of incoming gas flux, adiabatic temperature of gas combustion, reaction rate constant, diameter of porous body particles, reactor size and heat losses on maximal temperature of reactor, recuperation efficiency, combustion front position is investigated. It is shown that maximum temperature and recuperation efficiency of reactor has extremum in the field of incoming gas flow rate and porous body particle size parameters (for simulated configuration of reactor maximum corresponds to  $U_G \sim 2$  m/s and  $d_0 \sim 6$  mm). Numerical simulation shows non-monotonous character of maximal temperature and recuperation efficiency dependence from side heat losses of reactor. The obtained results can be used for construction optimization of practical VOC oxidation reactors. © 2006 Elsevier Ltd. All rights reserved.

*Keywords:* Filtration combustion (FC); Heat recuperation; Heat regeneration; Porous media; Volatile organic compounds (VOC); Oxidizer

## 1. Introduction

Air purification from Volatile Organic Compounds (VOC) remains actual problem facing chemical, nutrition, mining and other industries [1,2]. The widely spread VOCs – phenol, formaldehyde, acetone, benzole and other may be contained in ventilation gases of mines, paint shops, plastic extruder shops, in technological flue gases, etc. In many cases VOCs concentration is less than combustion lean limit concentration, but enough for self-sustained combustion in inert porous media. Combustion in inert porous media or filtration combustion (FC) provides effective heat recirculation and consequently low energy costs of the process [3–6]. In the case of sufficiently high concentration of VOCs ( $\sim 1$  mass%) the combustion process may be sustained due to the heat content of the pollutants and does not demand any additional fuels. In experiments by Takeno and Sato [7] in steady reactor with complicated

heat recuperation methane–air mixture combustion was realized at equivalence ratio as low as  $\Phi = 0.026$  (which is 20 times lower than lean limit combustion concentration for methane–air mixture). In the work [3,4] the regenerative porous media reactor was utilized for lean methane combustion. The stable combustion was achieved at equivalence ratio  $\Phi = 0.15$ .

One of the principal features of FC is internal heat recirculation in the combustion wave, due to heat exchange between gas and solid in the preheat zone of the combustion wave. Practical systems designed for the low calorific fuels combustion utilize schemes of external heat recirculation in addition to the internal one. These are heat recuperation by means of counter-flow heat exchange between incoming and exhaust gases and heat regeneration due to periodical reverse of flow direction. Both schemes are investigated in laboratory installations [3,4,8–10] and found their application in industrial VOCs oxidizers, produced by Thermatrix [10], ReEco-Stroem [11] and other companies. Physical aspects of the FC in inert porous media are discussed in [4,7,12,13] and other papers.

\* Corresponding author. Tel.: +375172842217; fax: +375172842212.  
E-mail address: [nick\\_gn@itmo.by](mailto:nick_gn@itmo.by) (N.N. Gnesdilov).

## Nomenclature

$a, a_0$	Arrhenius preexponential factor ( $\text{m}^3/(\text{mol s})$ )	$T_0$	initial temperature of the system (K)
$C_r$	efficiency of recuperation (dimensionless)	$U_G$	superficial gas velocity (m/s)
$C_1$	dimensionless losses from sidewall of reactor	$\mathbf{u}$	gas velocity vector (m/s)
$c_p$	heat capacity of gas ( $\text{J}/(\text{kg K})$ )	$X_i$	molar fraction of $i$ th component
$c_s$	heat capacity of porous carcass ( $\text{J}/(\text{kg K})$ )	$Y_i$	mass fraction of $i$ th component
$\mathbf{D}$	gas diffusivity tensor ( $\text{m}^2/\text{s}$ )	$z_1, z_2$	internal tube or reactor length (m)
$\mathbf{D}_d$	dispersion diffusivity tensor ( $\text{m}^2/\text{s}$ )	$z_f$	combustion front position (m)
$D_p, D_t$	longitudinal and transverse component of dispersion diffusivity tensor		
$D_g$	gas diffusivity coefficient, approximated by nitrogen properties ( $\text{m}^2/\text{s}$ )	<i>Greek symbols</i>	
$d_0$	diameter of porous carcass particle (m)	$\alpha$	heat exchange coefficient ( $\text{W}/(\text{m}^2 \text{K})$ )
$d_1$	internal tube diameter (m)	$\alpha_{\text{vol}}$	volumetric heat exchange coefficient ( $\text{W}/(\text{m}^3 \text{K})$ )
$d_2$	reactor diameter (m)	$\varepsilon$	emissivity of the porous carcass
$G$	gas mass flow rate ( $\text{kg}/\text{s}$ )	$\rho$	density ( $\text{kg}/\text{m}^3$ )
$h_i$	mass enthalpy of $i$ th chemical component	$\dot{\rho}_i$	mass generation rate of $i$ th component due chemical reactions ( $\text{kg}/\text{s}$ )
$\Delta h$	gas mixture heat of combustion ( $\text{J}/\text{kg}$ )	$\Lambda$	heat conductivity tensor ( $\text{W}/(\text{m K})$ )
$\mathbf{I}$	unit matrix	$\lambda$	conductivity or effective conductivity of porous carcass ( $\text{W}/(\text{m K})$ )
$k$	reaction rate ( $\text{m}^3/(\text{mol s})$ )	$\mu$	gas viscosity coefficient, approximated by nitrogen properties (Pa s)
$k_0, k_1$	filtration permeabilities	$\sigma$	Stefan–Boltzmann constant ( $5.67 \times 10^{-8} \text{ W}/(\text{m}^2 \text{K}^4)$ )
$M$	average molecular weight of gas ( $\text{kg}/\text{mol}$ )	$\tau$	unit vector with components $\tau_z, \tau_r$
$m$	porosity	$\Phi$	fuel/air equivalence ratio
$p$	pressure (Pa)	$\Omega$	surface of internal tube or reactor sidewall
$p_0$	outlet pressure (Pa)		
$Q_r$	heat flux via internal tube wall (W)	<i>Subscripts</i>	
$Q_1$	heat losses from side wall of reactor (W)	1	relates to internal tube
$R$	absolute gas constant	2	relates to reactor sidewall
$r$	radius (m)	g	gas
$S$	internal tube cross section ( $\text{m}^2$ )	$i$	$i$ th component of gas
$T$	temperature (K)	s	solid
$T_{\text{ad}}$	adiabatic temperature of combustion, $\Delta T_{\text{ad}} = T_{\text{ad}} - T_0$ (K)		

Though such type of reactors are under investigation and have a practical utilization, there is lack of obtainable publications concerned with detailed parametric study of these devices. The combined regenerator–recuperator scheme of VOC oxidizer was investigated in [14] numerically. Important parameters – maximal temperature of reactor,  $\text{NO}_x$  emission, effective ranges of gas flow rate and VOC concentration are compared for different types of reactor. It was shown that recuperative–regenerative scheme let one expand the range of operational flow rate and VOC concentration compared to stationary recuperative reactor.

Parametric study of filtration combustion reactor with electro heating elements was presented in [15]. The influence of gas flow rate, electrical heating elements position and power, and thermal isolation on maximal temperature in the system, unburned VOC concentration was investigated.

In this article numerical study of the steady-state recuperative (coaxial tubes type) reactor is performed. The influence of incoming gas flow rate, heat losses via side wall and other parameters on temperature and VOC burning

out is under investigation. Reactor recuperation efficiency and combustion front position were under consideration too. The chemical kinetics of the VOC oxidation is modeled by one-step Brutto model for methane combustion.

## 2. Problem statement

The system under investigation consists of two coaxial tubes, filled with ceramic particles – packed bed (Fig. 1). The reactor walls width is assumed to be zero in the model. The heat losses via side walls may be varied according to Newtonian law (7). At initial time instant porous body (Fig. 1, (4)) was preheated in order to ignite the gas mixture. VOC containing gas (Fig. 1, (1)) enters through central tube, heats up due to the heat exchange with porous body (Fig. 1, (4)) turns-around and goes out through the gap between internal tube and reactor body (Fig. 1, (2)). At certain temperature the VOC oxidation starts and xcombustion products heat up porous media and via it the incoming fresh gas mixture.

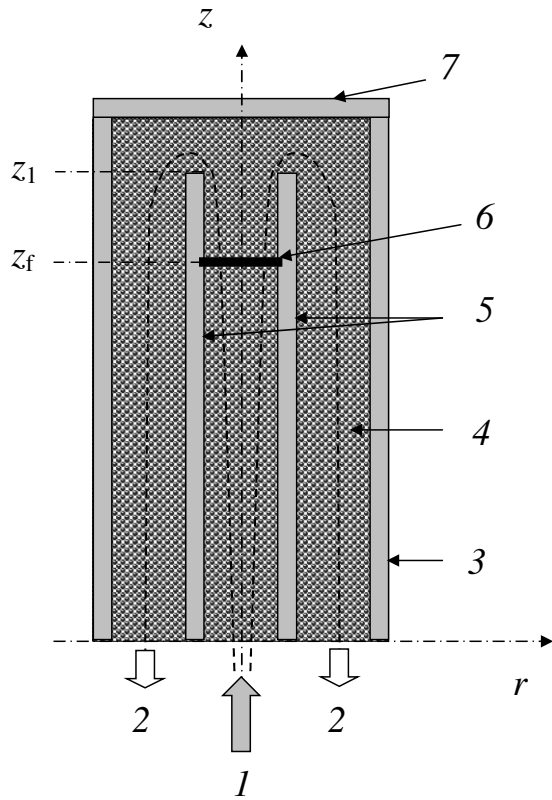


Fig. 1. Reactor scheme: (1) – incoming gases, with mass flow rate  $G$ , (2) – out coming gases, (3) – reactor side wall, (4) – porous media, (5) – internal tube, (6) – combustion front, (7) – cover,  $z_1$  – internal tube length,  $z_f$  – combustion front position.

Investigation of the system include parametric study where the main “target” parameters defining reactors design and operation regime are maximum temperature of the porous media, recuperation efficiency, front position and VOC oxidation completeness.

### 3. Governing equations

Conventional volume averaged approximation was used for the system simulation [14,16,17]. The set of equations included: the continuity and filtration equations for gas, the mass conservation equation for chemical components, the thermal conductivity equations for gas and the solid phase as well as the ideal gas state equation. Gas dispersion conductivity and diffusivity are used in the diffusion and conduction Eqs. (3) and (4). Radiation conductivity is taken into consideration in the heat conductivity Eq. (5). More detailed description of the mathematical model, boundary conditions and algorithms one can find in [14,16,17].

$$\frac{\partial \rho_g}{\partial t} + \nabla(\rho_g \mathbf{u}) = 0. \quad (1)$$

$$-\nabla p = \frac{\mu}{k_0} \mathbf{u} + \frac{\rho_g}{k_1} |\mathbf{u}| \mathbf{u}. \quad (2)$$

$$\rho_g \frac{\partial Y_i}{\partial t} + \rho_g \mathbf{u} \nabla Y_i - \nabla \rho_g \mathbf{D} \nabla Y_i = \dot{\rho}_i. \quad (3)$$

$$\rho_g c_p \frac{\partial T_g}{\partial t} + c_p \rho_g \mathbf{u} \nabla T_g - \nabla \lambda \nabla T_g = \frac{\alpha_{vol}}{m} (T_s - T_g) - \sum_i h_i \dot{\rho}_i. \quad (4)$$

$$(1 - m) \rho_s c_s \frac{\partial T_s}{\partial t} - \nabla(\lambda \nabla T_s) = \alpha_{vol} (T_g - T_s). \quad (5)$$

$$\rho_g = \frac{pM}{RT_g}. \quad (6)$$

The system (1)–(6) is added by boundary conditions for temperature, concentration and velocity. Tubes walls impermeability condition is applied for gas component concentration and velocity. Gas flow rate is fixed at the entrance cross section of the system. Constant pressure  $p = p_0$  at the exit conditions is used for the filtration equation solution. Adiabatic or Newtonian condition may be applied as boundary conditions for temperature (5):

$$-\lambda \frac{\partial T_s}{\partial r} \Big|_{r=0.5d_2} = \alpha (T_s|_{r=0.5d_2} - T_0). \quad (7)$$

The boundary conditions are presented in more details in [17].

Dispersion diffusion and conductivity of gas are taken into the account in transport equations for a gas (3) and (4):  $\mathbf{D} = D_g \mathbf{I} + \mathbf{D}_d$ , where  $\mathbf{D}_d = \begin{bmatrix} D_p \tau_z^2 + D_t \tau_r^2 & (D_p - D_t) \tau_z \tau_r \\ (D_p - D_t) \tau_z \tau_r & D_p \tau_r^2 + D_t \tau_z^2 \end{bmatrix}$  – dispersion diffusion tensor and  $\tau = \frac{\mathbf{u}}{|\mathbf{u}|}$ . Its component depends from gas velocity [18]:

$$D_p = 0.5d_0 |\mathbf{u}|; \quad D_t = 0.1d_0 |\mathbf{u}|. \quad (8)$$

$$\mathbf{A} = \lambda_g \mathbf{I} + c_p \rho_g \mathbf{D}_d \quad (9)$$

is dispersion conductivity tensor.

Radiation component of porous body conductivity is taken into the account in energy balance equation according to [19]:

$$\lambda = \lambda_s + \frac{16}{3} \left( \frac{0.666m}{(1-m)} \right) \varepsilon \sigma d_0 T_s^3. \quad (10)$$

Volumetric heat exchange coefficient between gas and porous body is [20]:

$$\alpha_{vol} = \frac{\lambda_g 6(1-m)}{d_0^2} \left[ 2 + 1.1 \left( \frac{\mu c_p}{\lambda_g} \right)^{1/3} \left( \frac{\rho_g u_g d_0}{\mu} \right)^{0.6} \right]. \quad (11)$$

The values of the system parameters in the standard case are presented in the Table 1. Diameters of tubes  $d_1$  and  $d_2$  were chosen in a way to give equal cross-section for incoming and outgoing gases.

VOC-containing gas was modeled by methane–air mixture with component ratio  $\text{N}_2:\text{O}_2:\text{CH}_4 = 80:20:1$  (equivalence ratio  $\Phi = 0.1$ ) in standard case. One step second order methane oxidation reaction was considered  $\text{CH}_4 + 2\text{O}_2 \xrightarrow{k} \text{CO}_2 + 2\text{H}_2\text{O}$ .

Oxidation rate was simulated by Arrhenius formula with the constants taken from [21]:

$$\frac{dX_{\text{CH}_4}}{dt} = -a X_{\text{CH}_4} X_{\text{O}_2} \exp(-15,640/T_g). \quad (12)$$

Table 1  
Standard values of the problem parameters

Parameter	Dimension	Value	Parameter description
$a$	$\text{m}^3/(\text{mol s})$	$2.17 \times 10^8$ $2.17 \times 10^7$ – $2.17 \times 10^{10}$	Preexponential factor in Arrhenius law (12) Varied
$c_s$	$\text{J/kg/K}$	1300	Porous body material heat capacity
$d_0$	$\text{mm}$	4.8	Packed bed particle diameter
$d_1$	$\text{cm}$	1–8 2.8	Varied Central tube diameter
$d_2$	$\text{m}$	1.8–3.6 0.04	Varied Reactor diameter
$m$	–	0.4	Porosity
$p_0$	$\text{Pa}$	$1.01325 \times 10^5$	Pressure at exit of reactor
$T_0$	$\text{K}$	300	Initial temperature of the system
$U_G$	$\text{m/s}$	1.0	Gas superficial velocity
$z_1$	$\text{m}$	0.1–5 0.37	Varied Central tube length
$z_2$	$\text{m}$	0.4	Reactor length
$\alpha$	$\text{W/m}^2/\text{K}$	0	Heat transfer coefficient between reactor side wall and ambient
$\alpha_{\text{vol}}$	$\text{W/m}^3/\text{K}$	0–10 $\sim 10^5$	Varied Volumetric heat transfer coefficient, calculated during simulation
$\varepsilon$	–	0.45	Emissivity of the packed bed particles
$\lambda_s$	$\text{W/m/K}$	1.87	Porous body material thermal conductivity coefficient
$\rho_s$	$\text{kg/m}^3$	3987	Porous body material density
$\Phi$	$\text{mol/mol}$	0.1	Fuel oxidizer equivalence ratio, corresponded $\Delta T_{\text{ad}} \approx 282.9 \text{ K}$
		0.03–0.3	Varied

The 2DBurner software package was used to solve two-dimensional problem (1)–(6) [17]. Normally after 5–15 min of physical time the system came to steady state. The steady-state solution was used to generate the data for parametric study of the system.

#### 4. Parametric study results and discussion

The most important for construction and exploitation of the VOC oxidation reactor parameters are VOC remains on exit, maximal gas and porous carcass temperatures and efficiency of heat recuperation  $C_r$ , determined as follows:

$$C_r = Q_r / \Delta h G. \quad (13)$$

Here  $Q_r = \int_{\Omega_i} \lambda \frac{\partial T}{\partial r} dS$  is conductivity heat flux from combustion products to fresh incoming gas via the internal tube wall and inter phase heat exchange,  $\Omega_i$  is a side wall surface of internal tube.

Combustion front position  $z_f$  at different parameters was studied because of  $z_f$  influence on recuperative heat flux  $Q_r$  and recuperation efficiency  $C_r$ . Actually, after VOC burn out in combustion front, temperature of gas does not increase downstream and in the case of adiabatic reactor remains constant until heat exchange with incoming gas starts at  $z < z_f$ . That is why recuperative heat flux via internal tube wall is zero at coordinate  $z \geq z_f$  and only part of the reactor length participates in the heat recuperation from out coming gases to incoming ones.

The simulation shows insignificant difference between the maximal temperature of gas and porous carcass and, therefore, only maximal temperature of porous carcass is presented on figures below. The data of VOC burn out are not presented in the paper. In all steady-state opera-

tional regimes the unburned methane concentration was less than  $10^{-6} \text{ mol/mol}$ .

Influence of gas velocity  $U_g$ , fuel/oxidizer equivalence ratio  $\Phi$ , reaction constant rate factor  $k$ , heat exchange coefficient  $\alpha$  on maximal porous body temperature  $T_{s,\text{max}}$ , front position  $z_f$  and heat recuperation efficiency  $C_r$  were investigated numerically. The data obtained for different  $\Phi$  were recalculated and presented as a function of  $\Delta T_{\text{ad}} = \Delta h / c_p$ , where heat capacity  $c_p$  of gas mixture assumed to be constant  $c_p = 1025 \text{ J/kg/K}$ .

##### 4.1. The influence gas velocity $U_g$ on maximal porous body temperature $T_{s,\text{max}}$ , front position $z_f$ and recuperation efficiency $C_r$

The graphs in Fig. 2(a) demonstrate non-monotonous behavior of  $T_{s,\text{max}}(U_G)$  and  $C_r(U_G)$  functions. The maximum of both functions lay near  $U_G = 2 \text{ m/s}$ . To investigate the physical nature of the non-monotonous behavior, we performed the simulation at reduced values of transport parameters  $D_p$ ,  $D_t$  and at  $\varepsilon = 0.2$ , it reduce effective diffusion and heat conductivity of gas and effective heat conductivity of porous carcass. Variation of the above parameters did not change significantly neither character of the curves nor absolute values of maximal temperature, efficiency of heat recuperation and front position.

##### 4.2. The influence of adiabatic temperature $\Delta T_{\text{ad}}$ on maximal porous body temperature $T_{s,\text{max}}$ , front position $z_f$ and recuperation efficiency $C_r$

The adiabatic combustion temperature is natural characteristic of the fuel mixture heat content. Its influence

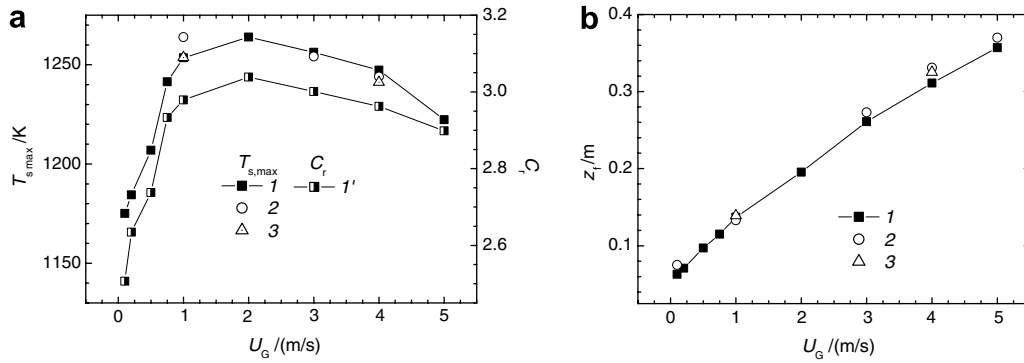


Fig. 2. Dependence of maximal temperature  $T_{s,max}$ , recuperation efficiency  $C_r$  – (a) and front position  $z_f$  – (b) on gas velocity  $U_G$ . 1, 1' – standard case; (2) – dispersion diffusion coefficients  $D_p, D_r$  decreased in 2.4 times; (3) – porous body emissivity  $\varepsilon = 0.2$ .

on main parameters of the reactor is illustrated in Fig. 3. The graphs in Fig. 3(a) show that maximal porous body temperature  $T_{s,max}$  and  $Q_r/z_f$  ratio increase nearly linearly with  $\Delta T_{ad}$  increase. Combustion front shifts upstream (to inlet) as is seen from Fig. 3(b). As it was shown above, recuperation efficiency  $C_r$  correlates with front position. Simulation show that combustion is impossible in the system for very low calorific mixtures  $\Delta T_{ad} \leq 49.4$  ( $\Phi \leq 0.03$ ).

4.3. The influence of reaction rate preexponential factor (12) (a) on maximal porous body temperature  $T_{s,max}$ , front position  $z_f$  and recuperation efficiency  $C_r$

Preexponential factor  $a$  characterizes reactivity of the fuel mixture. For alkanes it is not strongly varying factor, but taking in mind combustion of oxygen-, nitrogen-containing VOCs or other specific components this investigation may be of practical importance. We used dimensionless factor  $a/a_0$  as variable in our study. Simulation (Fig. 4) show decrease of the maximal temperature  $T_{s,max}$  with  $a$  growth. This “paradoxical” behavior has simple explanation. At increased reaction rate combustion processes goes faster and combustion zone shifts upstream. The consequent decrease of the front coordinate eliminate heat recuperation resulting in decrease of  $T_{s,max}$ . In the fast reaction limit ( $a/a_0 \rightarrow \infty$ ) the temperature will reach the value  $T_0 + \Delta T_{ad}$ . The quantitative presentation of this effect is given in Fig. 4.

4.4. The influence of porous body element diameter  $d_0$  on maximal temperature  $T_{s,max}$ , front position  $z_f$  and recuperation efficiency  $C_r$

It is known that porous body particle size is important parameter defining heat and mass transfer in porous media and FC dynamics. In the steady state regime of reactor the heat recuperation efficiency  $C_r$  as well as maximal carcass temperature are also determined by  $d_0$  (Fig. 5). For the case of the simulated system both parameters exhibit maximums at the value of  $d_0 \approx 6$  mm (Fig. 5(a)). Front position is nearly linear function of  $d_0$ . The front position shift downstream with increase of  $d_0$  (Fig. 5(a)) is explained by rather rapid decrease of the heat exchange coefficient (11). Note that normally the growth of  $z_f$  correlates with the growth of the recuperation coefficient  $C_r$ , but in the case of big elements of the porous media ( $d_0 > 6$  mm) heat exchange coefficient decreases too fast and recuperation coefficient  $C_r$  falls with it. This non obvious effect deserves thorough consideration when designing practical devices.

4.5. The influence of internal tube diameter  $d_1$  on maximal temperature  $T_{s,max}$ , front position  $z_f$  and recuperation efficiency  $C_r$

To determine the influence of geometrical factors on main parameters of reactor we varied diameter of internal

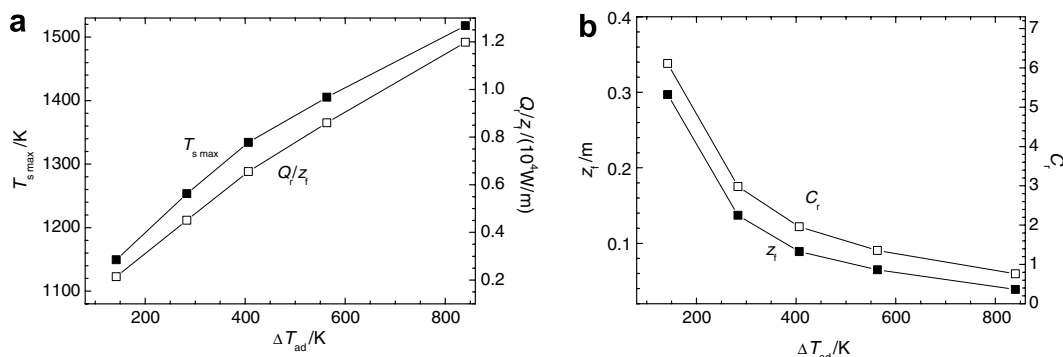


Fig. 3. Dependence of maximal temperature of porous carcass  $T_{s,max}$  – (a), relationship  $Q_r/z_f$  – (a), front position  $z_f$  – (b) and recuperation efficiency coefficient  $C_r$  – (b) on  $\Delta T_{ad}$ .



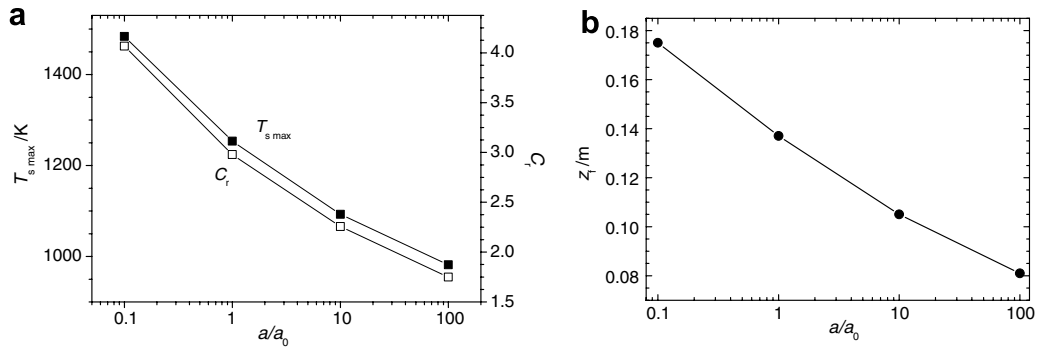


Fig. 4. Porous carcass maximal temperature  $T_{s,max}$  (line 1 at (a)), recuperation heat  $Q_r$  (line 2 at (a)), and flame front position coordinate  $z_f$  – (b) dependence on preexponential factor in the Arrhenius law (12)  $a/a_0$ . Here  $a_0 = 2.17 \times 10^8 \text{ m}^3/(\text{mol s})$ . All parameters are in SI units.

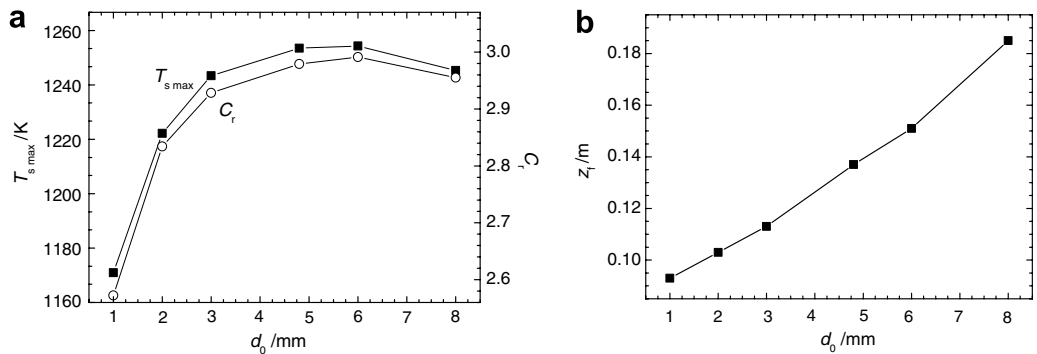


Fig. 5. Porous carcass maximal temperature  $T_{s,max}$  – (a), recuperation coefficient  $C_r$  – (a) and combustion front position  $z_f$  – (b) dependence on porous bed particles diameter  $d_0$ . Here  $d_0$  in mm other parameters in SI units.

tube, the external tube diameter being conserved. Simulation show (Fig. 6(b)) that combustion front position  $z_f$  shifts to the outlet with internal tube diameter  $d_1$  decrease. The principal physical factor here is growth of gas flow rate and velocity. Front position shift leads to growth of recuperation heat (as discussed earlier) and consequently  $T_{s,max}$ . Note that with further decrease of  $d_1$  to 1.6 cm ( $d_1/d_2 = 0.4$ ) combustion front bowed out from internal tube and steady combustion becomes impossible. It can be seen from comparison of Fig. 6(a) and (b), that  $C_r(d_1/d_2)$  and  $z_f(d_1/d_2)$  functions has similar character.

4.6. The influence of heat transfer coefficient  $\alpha$  on maximal temperature  $T_{s,max}$ , front position  $z_f$ , recuperation efficiency  $C_r$  and integral heat losses of reactor

Simulations were performed for the two ways of reactor feeding: 1 – gas input to the central tube and output through the gap between the tube and reactor body and 2 – reverse feeding. Non-dimensional losses from side wall of reactor was defined as  $C_1 = Q_l/\Delta hG$ , where  $Q_l = \int_{\Omega_2} \alpha(T_s - T_0)dS$  is heat flux from the reactor side wall to surroundings.

Simulation shows that the front position  $z_f$  and the heat losses from the reactor side wall do not depend considerably

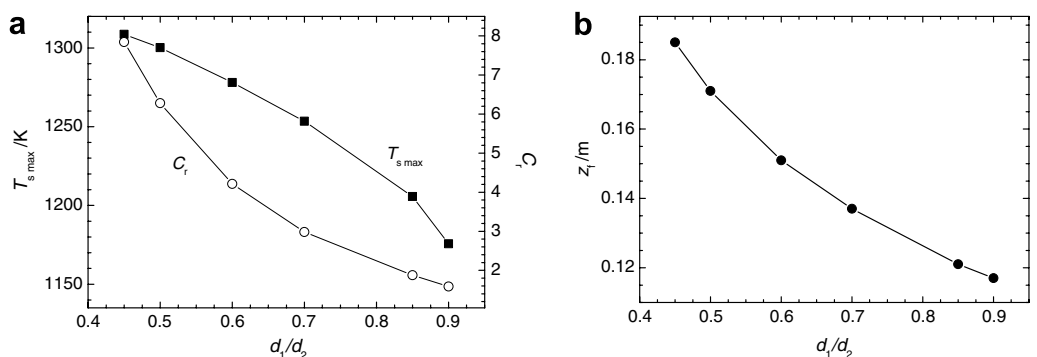


Fig. 6. Porous carcass maximal temperature  $T_{s,max}$  – (a), recuperation coefficient  $C_r$  – (a) and combustion front position  $z_f$  – (b) dependence on tube diameters ratio.

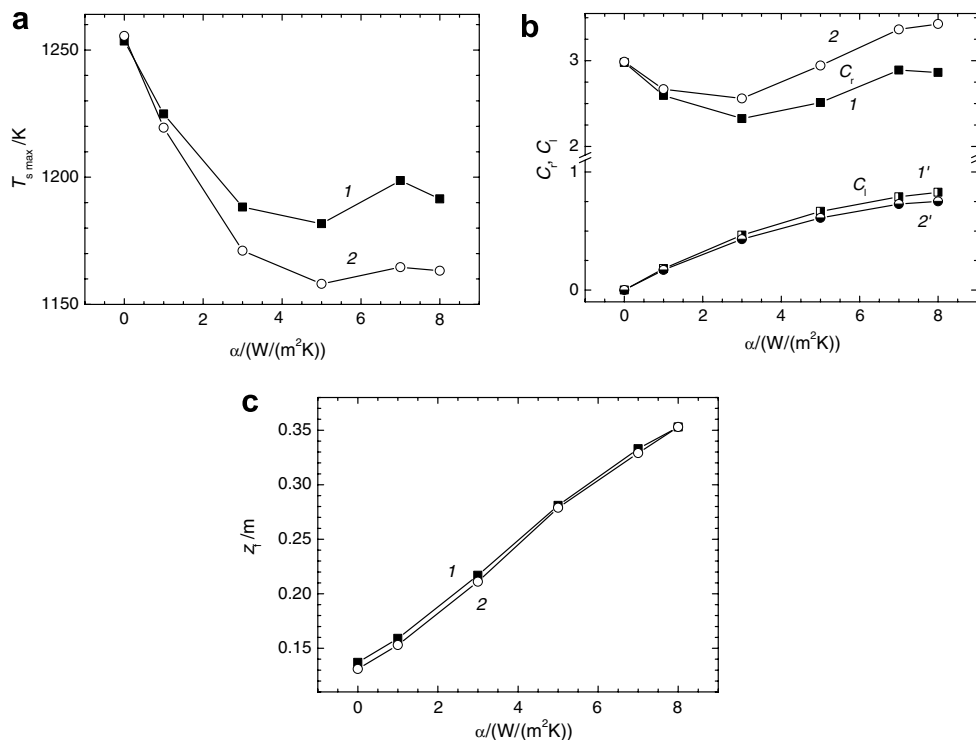


Fig. 7. Porous body maximal temperature  $T_{s,max}$  – (a) recuperation efficiency, heat losses from side wall of reactor  $C_r$  – (b) and front position  $z_f$  – (c) dependence on heat transfer coefficient  $\alpha$ . 1, 1' – gas income in the internal tube, 2, 2' – gas income in the gap between internal tube and reactor body.

on feeding way (Fig. 7(b) and (c), curves 1, 1' and 2, 2'). One can see (Fig. 7(a)) the increase of  $T_{s,max}$  and recuperation efficiency  $C_r$  within  $\alpha = 4\text{--}7 W/(m^2 K)$ . This behavior is explained by the increase of the front position coordinate  $z_f$ . Actually, the heat recuperation interface is limited by  $z < z_f$  area while the external heat losses  $C_1$  take place from the bigger part of the side wall of the reactor ( $z_f < z < z_2$ ). Increasing of  $z_f$  results, from one hand, in increase of the heat recuperation area, consequently, increases  $Q_r$  and, from the other hand, decrease area of the reactor heat exchanging with environment. These two factors lead to local  $T_{s,max}$  growth with  $\alpha$  increase. When the heat exchange coefficient  $\alpha$  reaches to  $10 W/m^3 K$ , steady regime of combustion became impossible.

## 5. Conclusion

Results of detailed simulation of the recuperative steady-state VOC oxidation filtration combustion reactor was presented in this paper. The maximum temperature, combustion front position and recuperation efficiency were investigated as functions of input gas flow rate, fuel mixture heat content, reaction rate constant, intensity of external heat losses of reactor and some other parameters.

It is shown in the paper that several important parametric dependencies have a non-monotonous hardly predictable nature determining optimal constructive parameters for the given technical application of reactor. For example, maximum temperature of porous media (necessary for effective VOC oxidation), may be reached in the field of

two parameters – porous body particles size and gas filtration rate. For the simulate system the optimal filtration velocity is estimated as  $U_g \approx 2$  m/s. Optimal diameter of porous body particles is  $d_0 = 6$  mm.

Internal tube diameter decreasing shifts front position to outlet of internal tube, increasing maximal temperature and recuperative efficiency of the reactor. From the other hand decrease of the tube diameter diminishes the operational range of gas flow rates. In the case of relatively low specific gas flow rates, reactor optimization may be performed in view of diminishing of  $d_1/d_2$  ratio.

Two geometries of the reactor gas feed was tested numerically – feed through internal tube and contrary via external tube. In conditions of non-adiabatic reactor gas feed via internal tube is preferable.

A set of questions important for practical devices exploitation and design, namely, flame front stability problem was not touched in this paper. According to [12] the stationary filtration combustion fronts are stable to 2D thermal and hydrodynamic perturbations if the hot zone is wider than tube diameter. In the case of flame stabilization near the end of the internal tube (maximising recuperation efficiency) the question of flame stability should be revised.

## Acknowledgements

The study was performed under the support of Fund for fundamental research of Republic of Belarus (Grant T05-259).

## References

- [1] R.J. Martin et al., Selecting the most appropriate HAP emission control technology, *The Air Pollution Consultant* 3 (2) (1993) 1.1–1.9.
- [2] Yu.S. Matros, A.S. Noskov, V.A. Chumachenko, *Catalytic recreation of industrial flue gases*. Nayka Publ., Novosibirsk, 1991, pp. 22–37 (in Russian).
- [3] F. Contarin, A.V. Saveliev, A.A. Fridman, L.A. Kennedy, *Int. J. Heat Mass Transfer* 46 (2003) 949–961.
- [4] L.A. Kennedy, A.A. Fridman, A.V. Saveliev, Superadiabatic combustion in porous media: wave propagation, instabilities, new type of chemical reactor, *Int. J. Fluid Mech. Res.* 22 (1995) 1–26.
- [5] J.G. Hoffman, R. Echigo, H. Yoshida, S. Tada, Experimental study on combustion in a porous media with a reciprocating flow system, *Combust. Flame* 111 (1997) 32–46.
- [6] W.D. Binder, R.J. Martin, The Destruction of Air Toxic Emissions by Flameless Thermal Oxidation, Presented at 1993 Incineration Conf., Knoxville, Tennessee, 4 May, 1993.
- [7] T. Takeno, K. Sato, An analytical study on excess enthalpy flames, *Combust. Sci. Technol.* 20 (1979) 73.
- [8] M.K. Drayton, A.V. Saveliev, L.A. Kennedy, A.A. Fridman, Y.E. Li, Superadiabatic partial oxidation of methane in reciprocal and counterflow porous burners, in: *Proc. of The 27th Symp. Int. on Combust.* Pittsburg, PA. 1998, pp. 1361–1367.
- [9] A.N. Migoun, A.P. Chernukho, S.A. Zhdanok, Numerical modeling of reverse-flow catalytic reactor for methane partial oxidation, in: *Proc. of the Non-equilibrium processes and their applications*, V Int. School-seminar. Minsk 2000, pp. 131–135.
- [10] Available from: <<http://www.thermatrix.com/>>.
- [11] Available from: <<http://www.eco-web.com/>>.
- [12] K.V. Dobrego, S.A. Zhdanok (in Russian), in: *Physics of filtration combustion of gases*, HMTI Publishers, Minsk, 2002.
- [13] K. Hanamura, R. Echigo, S. Zhdanok, Superadiabatic combustion in a porous medium, *Int. J. Heat Mass Transfer* 36 (13) (1993) 3201–3209.
- [14] K.V. Dobrego, N.N. Gnesdilov, I.M. Kozlov, V.I. Bubnovich, H.A. Gonzalez, Numerical investigation of the new regenerator–recuperator scheme of VOC oxidizer, *Int. J. Heat Mass Transfer* 48 (2005) 4695–4703.
- [15] N.N. Gnesdilov, K.V. Dobrego, I.M. Kozlov, E.S. Shmelev, Numerical study and optimization of the porous media VOC oxidizer with electric heating elements, *Int. J. Heat Mass Transfer* 49 (2006) 5062–5069.
- [16] K.V. Dobrego, I.M. Kozlov, S.A. Zhdanok, N.N. Gnesdilov, Modeling of diffusion filtration combustion radiative burner, *Int. J. Heat Mass Transfer* 44 (2001) 3265–3272.
- [17] Dobrego K.V., Kozlov I.M., Gnesdilov N.N., Vasiliev V.V., 2DBurner – software package for gas filtration combustion systems simulation and gas non-steady flames simulation, *Heat and Mass Transfer Institute. Minsk 2004. Preprint N1.*
- [18] N. Wakao, S. Kagueli, *Heat and mass transfer in a packed beds*, Gordon and Breach, New York, 1982.
- [19] O.E. Gorelik, V.V. Levdansky, V.G. Leitsina, N.V. Pavlyukevich, On radiation absorption in a high-porous material layer, *J. Eng. Phys. Thermophys.* 50 (1986) 999–1004.
- [20] M. Kaviani, *Principles of Heat Transfer in Porous Media*, Springer-Verlag, New York, Berlin, Heidelberg, 1995.
- [21] V.Ya. Basevich, A.A. Belyaev, S.M. Frolov, “Global” kinetic mechanism for turbulent reacting flow modeling. Part 1. Main chemical process of heat release, *Chem. Phys.* 17 (9) (1998) 117–129 (in Russian). M. Nauka.